

Comments by Rafael Repullo on

# **Intermediaries as Safety Providers**

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## Purpose of paper (i)

- New theory of financial intermediation
  - Based on demand for “safety”
  - Interpreted as subsistence level of consumption
- Consumers differ in access to safety
  - Heterogeneous (private) return to storage
- Consumers also have access to a public risky investment

## Purpose of paper (ii)

- Intermediaries can invest in risky asset
  - To satisfy demand for safety
  - By consumers with low storage return
- How can you provide safety by investing in a risky asset?
  - Exploit non-zero liquidation return
  - Split cash flows by seniority
  - Consumers with low storage return get senior debt
  - Consumers with high storage return get junior debt/equity

# Main results

- Portfolio choice in autarky
  - All agents use storage + invest in risky asset
- First-best improves upon autarky
  - Reduce storage by consumers with low return
  - Provide safety by liquidation returns
- First-best can be implemented by intermediaries
  - Pooling resources enables private provision of safety
  - No role for diversification (Diamond)
  - No role for liquidity insurance (Diamond and Dybvig)

# Main comments

- Model assumes that intermediaries can only invest in risky asset
  - Strange assumption given role in providing safety
- Model assumes arrival of information at interim date
  - To justify the emergence of demand deposits
  - But this is not needed for the core of the argument
- Paper is short, but not easy to read
  - Some loose ends in the implementation section

# What am I going to do?

- Consider a simple version of the model
  - With no arrival of information at interim date
- Briefly comment on some results of paper
  - Public provision of safety
- Briefly comment on some related work
  - Allen and Gale (1988)

# **Part 1**

## **A simple version of the model**

# Model setup

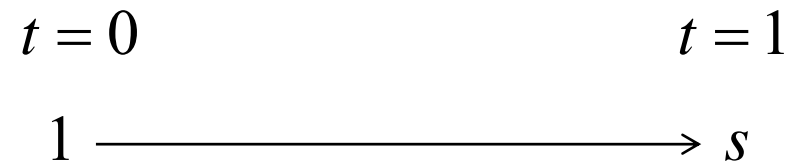
- Two dates ( $t = 0, 1$ )
- Consumer characterized by
  - Unit endowment at  $t = 0$
  - Preferences for consumption  $c_1$  at  $t = 1$

$$u(c_1) = \begin{cases} c_1 & \text{if } c_1 \geq S \\ -\infty & \text{otherwise} \end{cases}$$

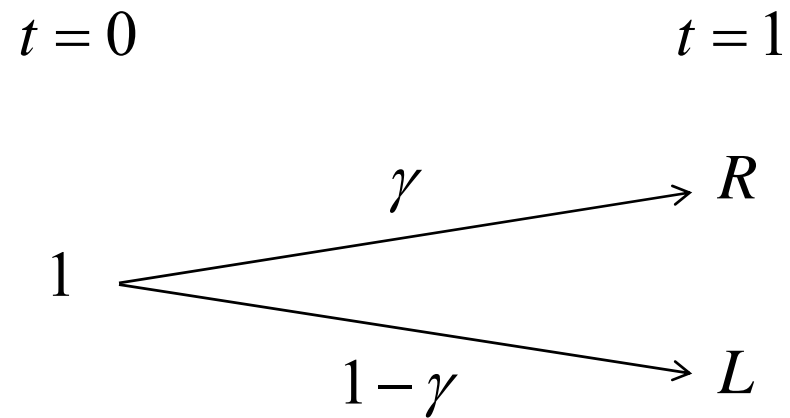


# Investments

- Private safe investment (storage)



- Public risky asset



# Assumptions

$$0 < L < S < s < \gamma R + (1 - \gamma)L$$

- Storage return  $s$  is lower than expected return of risky asset
  - Risky asset is better
  - But does not guarantee minimum consumption  $S$
- Storage guarantees minimum consumption  $S$ 
  - Some storage will be optimal

# Optimal investment

- Let  $x \in [0, 1]$  denote investment in storage  
→  $1 - x$  invested in risky asset

- Consumer's problem

$$\max_x [xs + (1 - x)(\gamma R + (1 - \gamma)L)]$$

$$\text{subject to } xs + (1 - x)L \geq S$$

- Solution: minimum  $x$  that satisfies the constraint

$$\hat{x} = \frac{S - L}{s - L}$$

## Two types of consumers

- Suppose that consumers may differ in storage return
  - Type  $H$  has high return  $s_H$
  - Type  $L$  has low return  $s_L < s_H$
- As before we assume

$$0 < L < S < s_L < s_H < \gamma R + (1 - \gamma)L$$

# First-best allocation

- Planner chooses  $x_L \in [0,1]$  and  $x_H \in [0,1]$  to maximize output subject to subsistence constraint

$$\max_{x_L, x_H} [x_L s_L + x_H s_H + (2 - x_L - x_H)(\gamma R + (1 - \gamma)L)]$$

$$\text{subject to } x_L s_L + x_H s_H + (2 - x_L - x_H)L = 2S$$

# Numerical illustration

- Suppose that

$$0 < L = 0.4 < S = 0.5 < s_L = 0.8 < s_H = 1.2$$

$$\gamma = 0.75 \text{ and } R = 2 \rightarrow \gamma R + (1 - \gamma)L = 1.6$$

# Autarky allocation

- Storage under autarky

$$\hat{x}_L = \frac{S - L}{s_L - L} = \frac{0.5 - 0.4}{0.8 - 0.4} = 0.25$$

$$\hat{x}_H = \frac{S - L}{s_H - L} = \frac{0.5 - 0.4}{1.2 - 0.4} = 0.125$$

- Consumption under autarky

$$\hat{u}_L = \hat{x}_L s_L + (1 - \hat{x}_L)(\gamma R + (1 - \gamma)L) = 1.40$$

$$\hat{u}_H = \hat{x}_H s_H + (1 - \hat{x}_H)(\gamma R + (1 - \gamma)L) = 1.55$$

# First-best allocation

$$\max_{x_L, x_H} [3.2 - 0.8x_L - 0.4x_H]$$

$$\text{subject to } 0.8 + 0.4x_L + 0.8x_H = 2S = 1$$

- Solving for  $x_H$  in the constraint gives

$$x_H = 0.25 - 0.5x_L$$

- Substituting it into objective function gives

$$\max_{x_L} [3.1 - 0.6x_L] \rightarrow x_L^* = 0 \text{ and } x_H^* = 0.25$$



# First-best vs. autarky allocation

- Comparison of first-best with autarky allocation
  - Type  $L$  reduces storage to zero (relative to autarky)
  - Type  $H$  increases storage from 0.125 to 0.25
  - Total consumption increases from 2.95 to 3.1

# Implementing first-best allocation

- Implementation by intermediary offering debt and equity
- Implementation constraints
  - Both types should be better off than in autarky
  - $x_L^* = 0$  implies that type  $L$  prefers debt to storage
  - $x_H^* s_H = 0.3 < S$  implies that type  $H$  is indifferent between debt and storage
  - Expected equity return must be sufficiently high

# Comments on the implementation

- One can show that previous constraints can be satisfied
  - What happens in model with continuum of types?
- One important unresolved issue (also in paper)
  - How are the output gains distributed among types?

## **Part 2**

# **Public provision of safety**

# Public provision of safety

- Paper addresses impact of changes in supply of safe assets
  - Interesting topic (given literature on scarcity of safe assets)
- This is done through change in low storage return  $s_L$ 
  - Too much of a reduced form!
  - May be better to analyze effects of change in subsistence  $S$

# Effect of change in subsistence consumption

- Suppose that reduced public provision of safety increases  $S$
- Effect on first-best allocation

$$\max_{x_L, x_H} [3.2 - 0.8x_L - 0.4x_H]$$

$$\text{subject to } 0.8 + 0.4x_L + 0.8x_H = 2(S + \Delta S) = 1.2$$

→ Operating as before this reduces to

$$\max_{x_L} [3 - 0.4x_L] \rightarrow x_L^* = 0 \text{ and } x_H^* = 0.5$$

# Effect of change in subsistence consumption

- Effect of an increase in  $S$ 
  - Type  $H$  increases storage from 0.25 to 0.5
  - Lower investment in risky asset
  - Lower private provision of safety (more storage)
  - Total consumption goes down from 3.1 to 3
- In contrast with results in the paper!

## **Part 3**

**Comment on some related work**



## Allen and Gale (1988)

“This article develops a model in which the instruments that are traded are chosen optimally and the economy’s market structure is endogenous. It is shown that the **firm’s income stream should be split** so that in every state all **payoffs are allocated to the security held by the group that values it most.**”

- Is it not the same story, with “banks” instead of “firms”?  
→ Deserves a serious discussion

## Some results of Allen and Gale (1988)

- Equilibrium is constrained efficient
  - But first-best risk-sharing is not achieved
- When firm issues two securities each one targeted to clientele
  - Firm's output allocated to clientele that values it most
- Optimal securities need not be debt and equity
- No short-sales assumption is critical

# **Concluding remarks**

# Concluding remarks

- Interesting idea to build theory of intermediation
  - New approach to model demand for safety
- Need to tidy up some results
  - In particular on implementation of first-best allocation
- Need to relate to previous work by Allen and Gale
  - In what sense are we talking about “banks”?
- Model should be able to incorporate other theories
  - In particular those related to provision of liquidity

# References

- Allen, F., and D. Gale (1988), “Optimal Security Design,” *Review of Financial Studies*.
- Allen, F., and D. Gale (1991), Arbitrage, Short Sales and Financial Innovation,” *Econometrica*.
- Allen, F., and D. Gale (1994), *Financial Innovation and Risk Sharing*.